

# Methods of rf Current Drive

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Radio frequency waves can penetrate thermonuclear plasmas, depositing momentum and energy with great selectivity: in select resonant ions or electrons, in select resonant regions, and with select momentum.



# TFTR

Tokamak Fusion Test Reactor (1989)

# Driving a Toroidal Current with Waves

Note:  $\text{curl } J \neq 0$

How are these plasma  
waves excited?

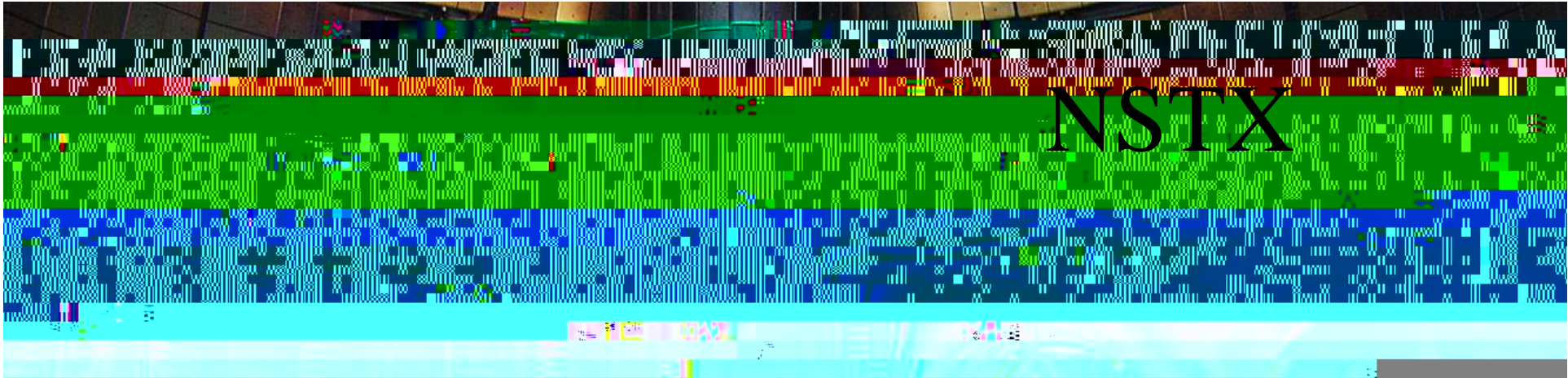
Example:

Tore Supra LH Grill

4 MW

1000 s

3.7 GHz



NSTX



## Uses of RF Waves in Magnetic Confinement Fusion Devices seeking ever increasing control of plasma

1970's: Heat Plasma to Thermonuclear Temperature:

Ion Cyclotron, Lower Hybrid, Electron Cyclotron Waves

1980's: Drive Mega-amps of plasma current

LHCD, ECCD, MiCCD current drive

1990's: More detailed positioning of plasma current

Use LHCD, ECCD to control of NTM, sawteeth, plasma current profile

1990's: Exploit coupled diffusion of particles in velocity and position  
° ! ~ Channeling effect"

**Trend to ° phase space engineering" !**

Detailed control of rf-induced fluxes in 12-D!

!Select particles in 6D velocity-configuration space !

!Select flux vector in 6D velocity-configuration space !

# Early Current Drive Work

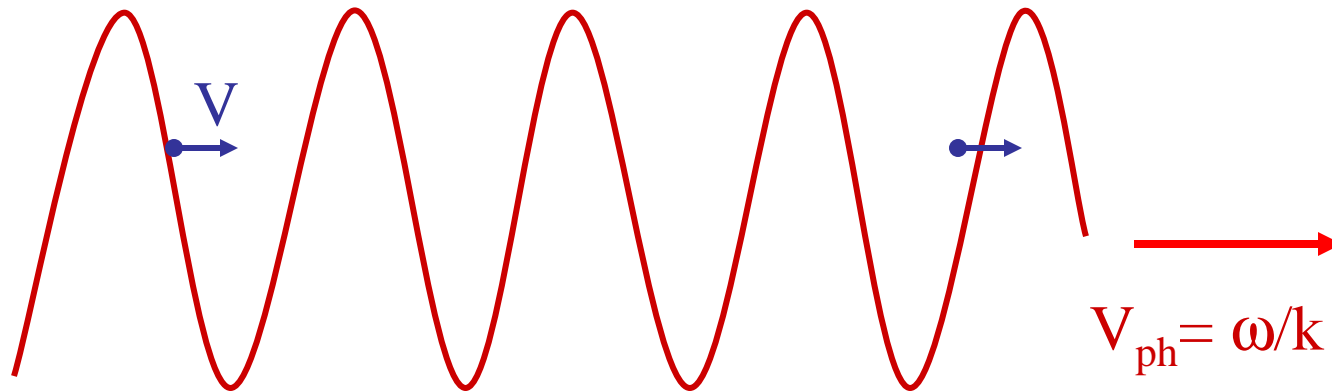
1952 Thoneman *et al.* -- glass tube

1966 Yoshikawa and Yamato -- C- Stellarator (200 s)

1970 Ohkawa -- Neutral beams,  $v < v_T$

1971 Wort -- waves  $v_{ph} < v$

# (Resonant) Radio Frequency (RF) Current Drive Effect



$$\mathbf{v} \quad \mathbf{v} \quad \mathbf{v}$$

$$\mathbf{J} = en \mathbf{v}$$

$$\mathbf{E} = m n \mathbf{v} \mathbf{v}$$

$$P_D = \mathbf{v} \Delta E$$



## Example of Resonance: The Traveling Plasma Wave

$$\vec{E} = -4\pi e(n_0 - n_e) = -4\pi e\tilde{n} \quad \text{Poisson's equation}$$

$$\frac{\partial}{\partial t} n_e + n_e v = 0 \quad \text{Particle conservation}$$

$$\frac{\partial}{\partial t} n_e m v + n_e m v v = eE \quad \text{Momentum conservation}$$

$$\frac{\partial^2}{\partial t^2} \tilde{n} - \frac{\partial^2}{\partial p^2} \tilde{n} = 0$$

! "\$%#&' \$()""#\* +,&

# Electron acceleration in a plasma wave

# Accelerating Gradient in Plasma

## Conventional Accelerator

Gradients  $\sim 20$  MeV/m at 3GHz

1 TeV Collider requires 50 km

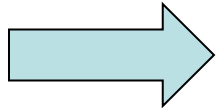
Peak gradients limited by breakdown

## Plasma Accelerator

High fields, No breakdown

(Tajima and Dawson, 1979)

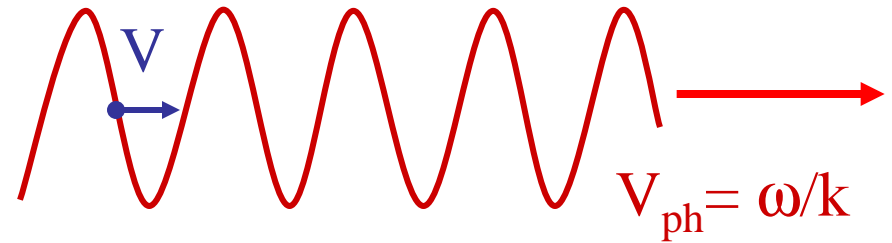
### Example



$$n_0 = 10^{18} \text{ cm}^{-3}$$

$$eE = 100 \text{ GeV/m}$$

Note: For  $v \ll c$ , 
$$\frac{v_{osc}}{c} \approx \frac{\tilde{n}}{n_0}$$



$$\nabla \cdot \vec{E} = -4\pi e\tilde{n}$$

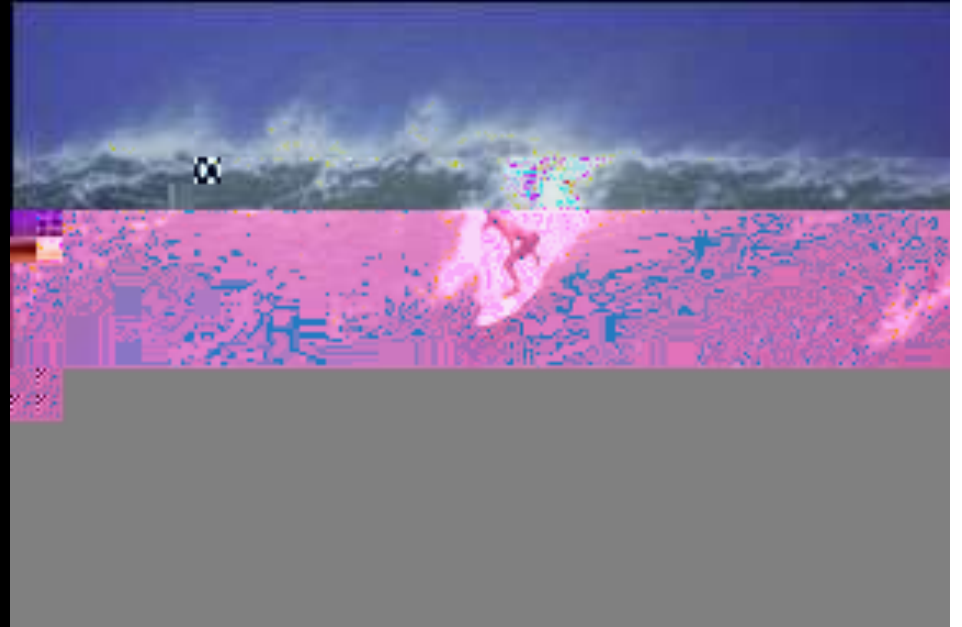
$$\tilde{n}_{MAX} \approx n_0$$

$$k = \frac{\omega}{c}$$

$$eE_{MAX} \approx \sqrt{n_0} \text{ GeV/cm}$$

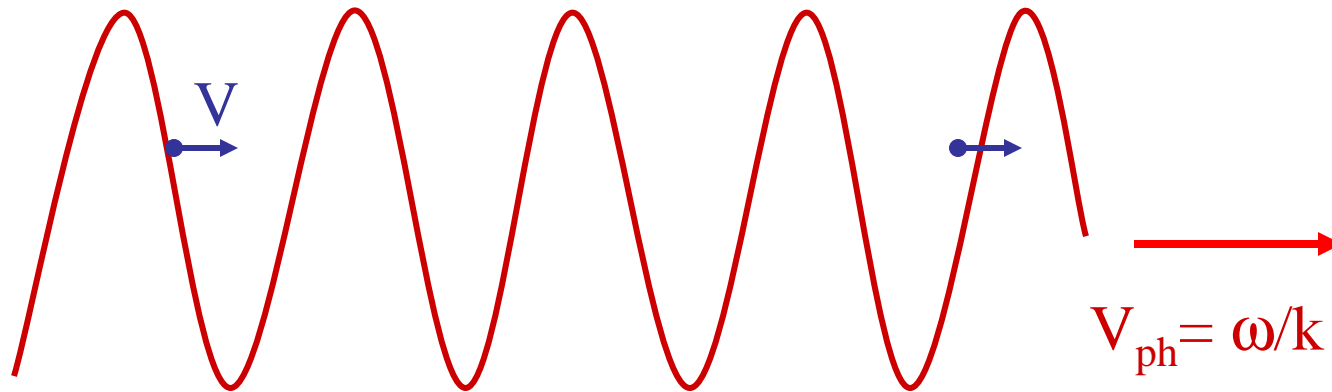
Particles accelerated to relativistic energies, even as plasma motion is not

- . \$+ , # , /&0123. 2\$



Not-resonant surfers  $V \neq V_{ph}$

# (Resonant) Radio Frequency (RF) Current Drive Effect



$$\mathbf{v} \quad \mathbf{v} \quad \mathbf{v}$$

$$\mathbf{J} = en \mathbf{v}$$

$$\mathbf{E} = m n \mathbf{v}$$

$$P_D = \mathbf{v} \Delta E$$

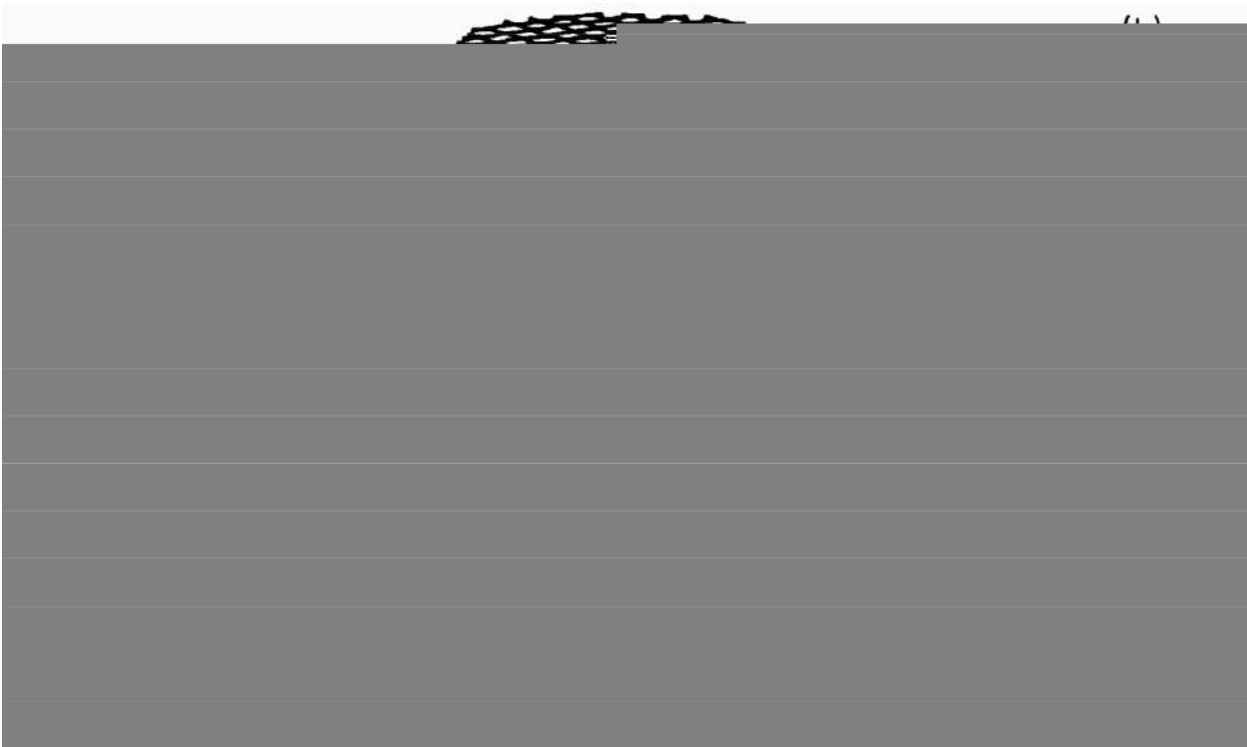
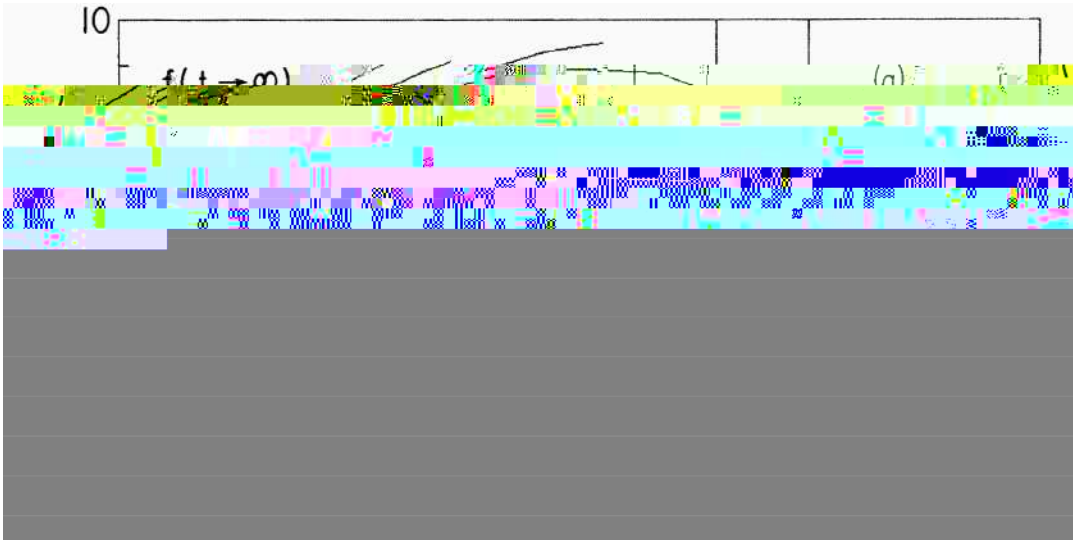


# RF Methods of Heating and Current Drive

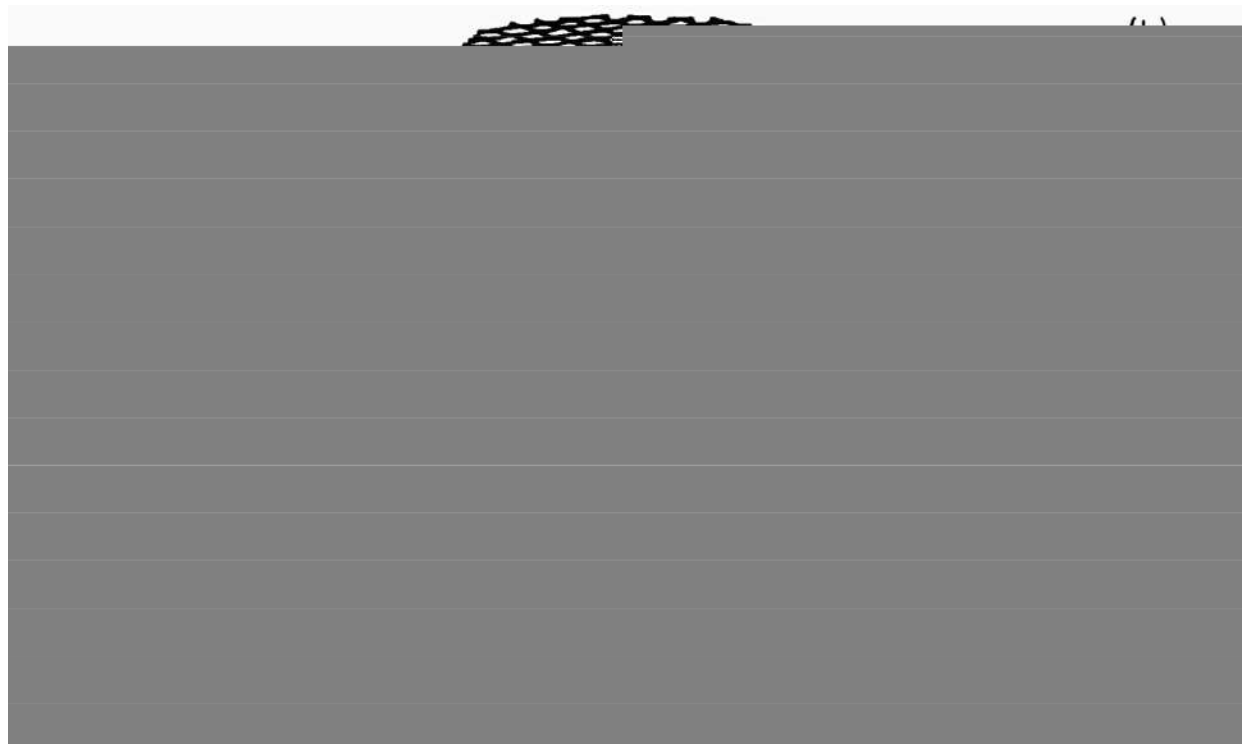
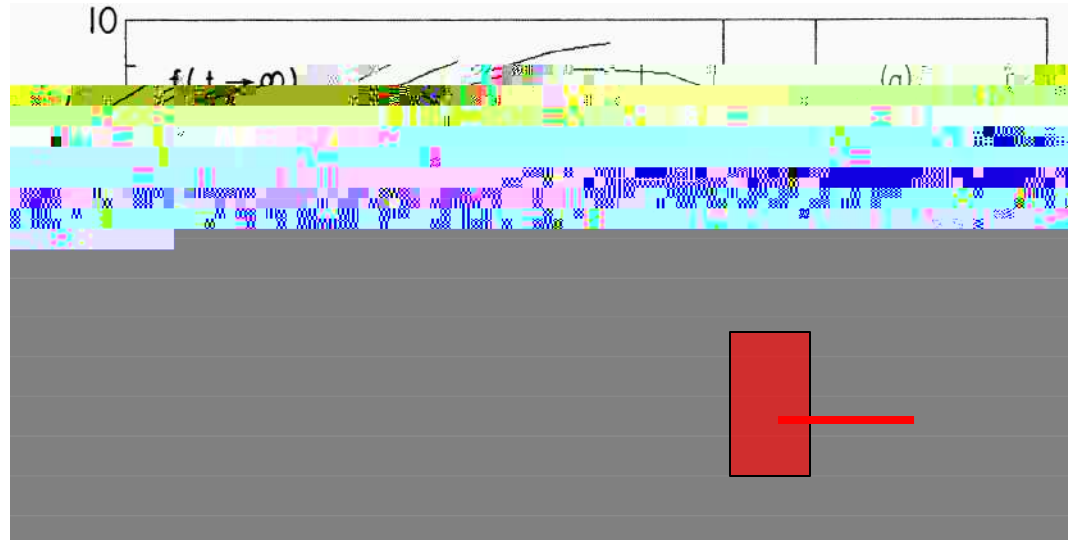




# Electron Distribution Function -- LHCD



# Electron Distribution Function



# Progress in Current Drive

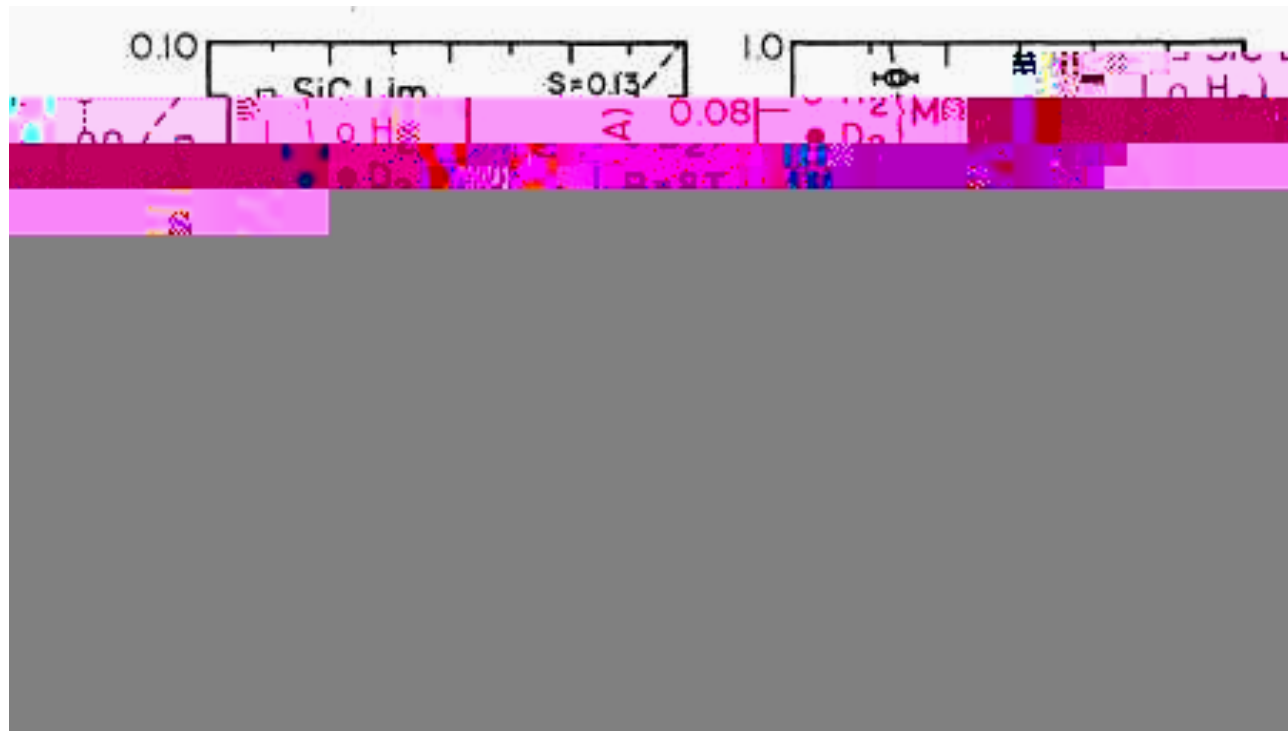


JET (2001)

# Alcator C

Current drive efficiency at B=8T shows  $n^{-1}$  scaling

Porkolab et al, 1984



Line-averaged density  
times current vs. power

Efficiency vs. density

# Theory and Demonstration of the Current Drive Effect with PLT Data

$P_{el}$  is power into stored magnetic  
energy

$$P_{el}/P_{rf}$$

*Ramp-up:  $E < 0$*



Karney, Fisch and Jobes  
(1985)

Corroborated on:

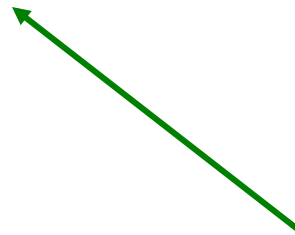
ASDEX: Leuterer (1991)

PBX: Giruzzi; Bernabei (1997)

HT-7: Chen (2005)

Also note ECCD consistency

DIII-D: Petty (2002)



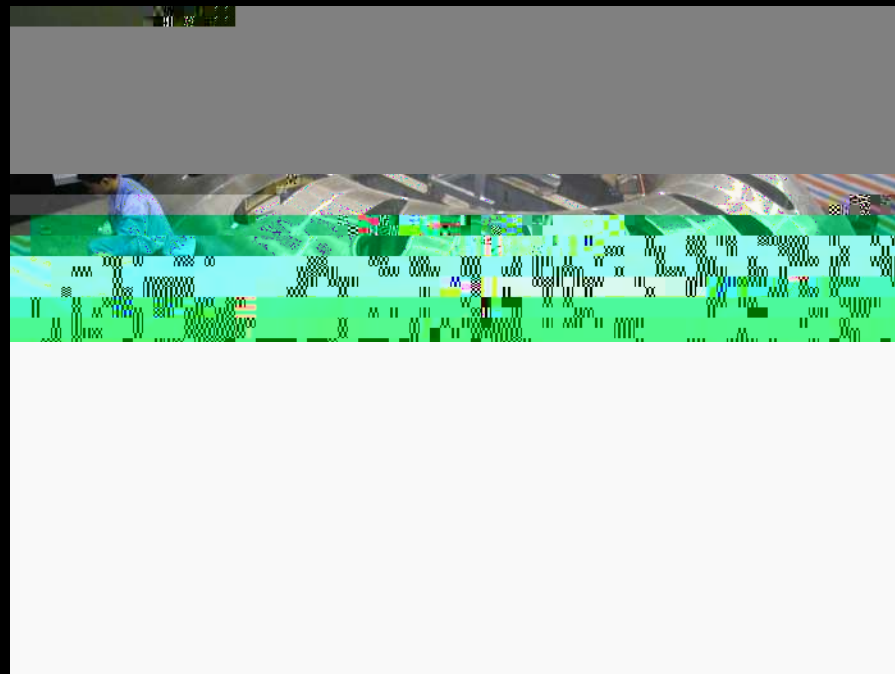
*Steady State:  $E = 0$*

$$v_{ph}/v_R$$

$v_R$  = runaway velocity

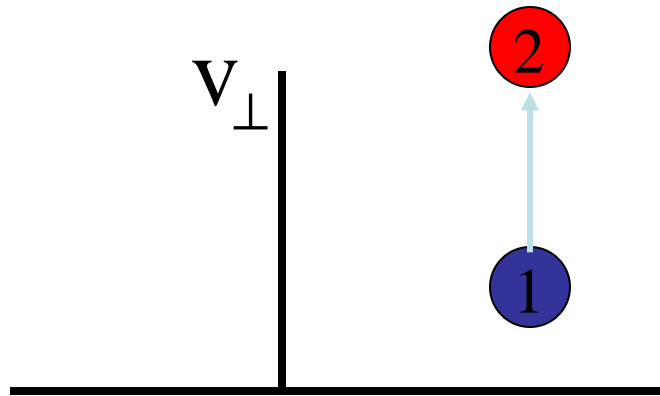
**Verification *in detail* proves classical picture of electron collisions!**

# Tokamak East



LHCD with very long pulse -- time scales for pinch effects  
Low frequency ICRF with 4T (internal mode excitation)

# Electron Cyclotron Current Drive Effect



$$! - \vec{k} \cdot \vec{v} \quad n\Omega$$

$$\Omega \equiv$$





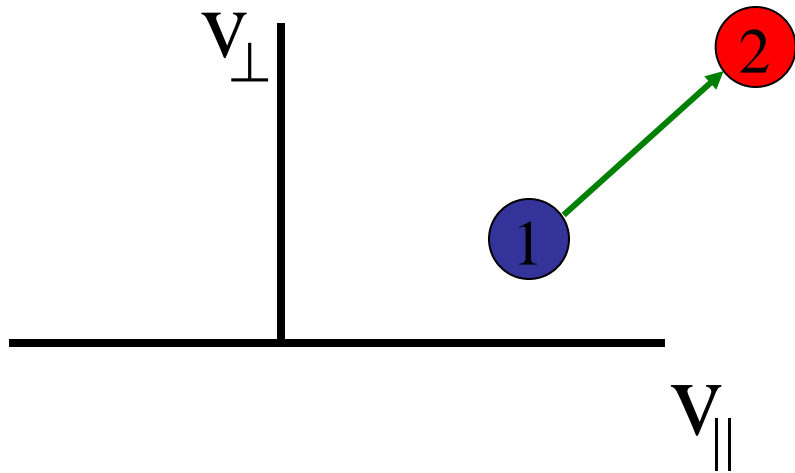
## Langevin Equations

$$\frac{\partial f}{\partial t} = C(f, f) - C(f, f_i) + C(f, f_i) - \frac{\Gamma}{2v^3} \frac{\partial}{\partial \mu} (1 - \mu^2) \frac{\partial f}{\partial \mu}$$

$$\frac{\partial v}{\partial t} = -\frac{\Gamma}{2v^3} v \quad \frac{\partial \langle \mu \rangle}{\partial t} = -\frac{\partial}{\partial t} \frac{\Gamma}{2v^3} \int \mu \frac{\partial}{\partial \mu} (1 - \mu^2) \frac{\partial f}{\partial \mu} + \frac{\Gamma}{2v^3} (1 - Z_i) \langle \mu \rangle$$

$$\frac{\partial \langle \mu \rangle}{\partial t} = (1 - Z_i) \langle \mu \rangle$$

# Generalized RF Current Drive Effect



$$! - \vec{k} \cdot \vec{v} \quad n\Omega$$

$$J \int d^3v \bar{S} \cdot \bar{\nabla} \Psi$$

$$P_D \int d^3v \bar{S} \cdot \nabla$$

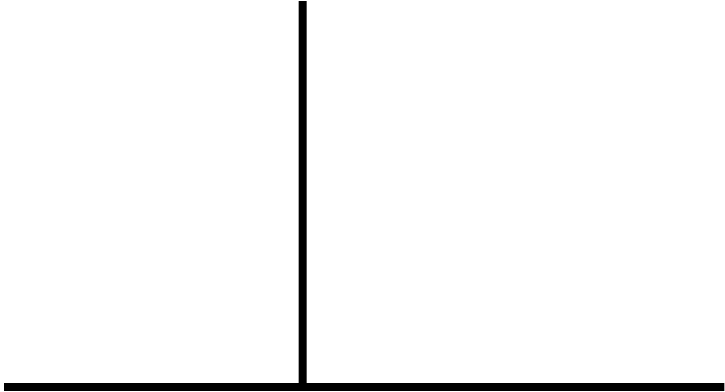
# Generalized Transport Quantities

Associate transport quantity with each point in 2D velocity space

1. Current Drive Efficiency

2. Runaway Probability

3. Energy flow to stored magnetic energy


$$W_{el} = \int_0^{\infty} ev \cdot E dt$$

# Conclusions From Current Drive Campaign

## A.! Current drive effect established as a tool

- 1.! Precise control over RF Absorption.
- 2.! New transport quantities demonstrated.
- 3.! Contemplate steady-state tokamak reactors.

## B.! Fundamental physics established

- 1.! Slowing down equations of fast electrons not hitherto tested since Spitzer conductivity not sensitive to fast electrons.
- 2.! But the transport quantities verified are far more detailed than Spitzer conductivity (integrated quantity).
- 3.! Verification *in detail* therefore resolved the question whether classical Coulomb collisions govern superthermal electrons!

## Examples of Further Development of RF Current Drive

JT-60 and JT60-U (Japan) -- 3 MA LHCD, 800 kA ECCD, ITB sawteeth stabilization (2001)

JET (England) -- 3 MA LHCD, ITB with LHCD, Minority Species CD. ITB

Tore Supra (France) -- 1000 s LHCD, ITB; 330 s, 1 GJ, LHCD (2004), ECCD Synergy

C-Mod tokamak (MIT) : LHCD

TRIAM (Japan): several hours LHCD

T-10 (Russia): ECCD, sawteeth

TCV tokamak --- ECCD steady state, sawteeth

ASDEX (Germany): ECCD stabilization of tearing modes

Wendelstein 7-AS Stellarator: ECCD

Frascati FT-U (Italy): LHCD, ECCD stabilization of sawteeth, tearing modes

General Atomics DIII-D tokamak; ECCD, ITB, mode suppression

Princeton spherical torus: NSTX (HHFWCD)

New Steady-State Superconducting Lower-hybrid driven

SST (India)

KSTAR (Korea)

HT-7 and HT7-U "East" (China)

## Superconducting tokamak TRIAM-1M (Kyushu, Japan)

*TRIAM, Advanced Fusion Research Center  
Courtesy H. Zushi*

**Major radius!                      0.84 m!**

**Minor radius!                      0.12 m!**

**Toroidal field!            8 T (Steady State)!**

**TF coils : Nb<sub>3</sub>Sn (superconductor)**

**PF coils : Cu (normal conductor)**

### **Current drive**

**Lower Hybrid Waves (CW)**

**8.2 GHz 400 kW 16 Klystrons**

**2.45 GHz 50 kW 1 Klystron**

**Electron Cyclotron Waves**

**170 GHz 200 kW 5 sec**

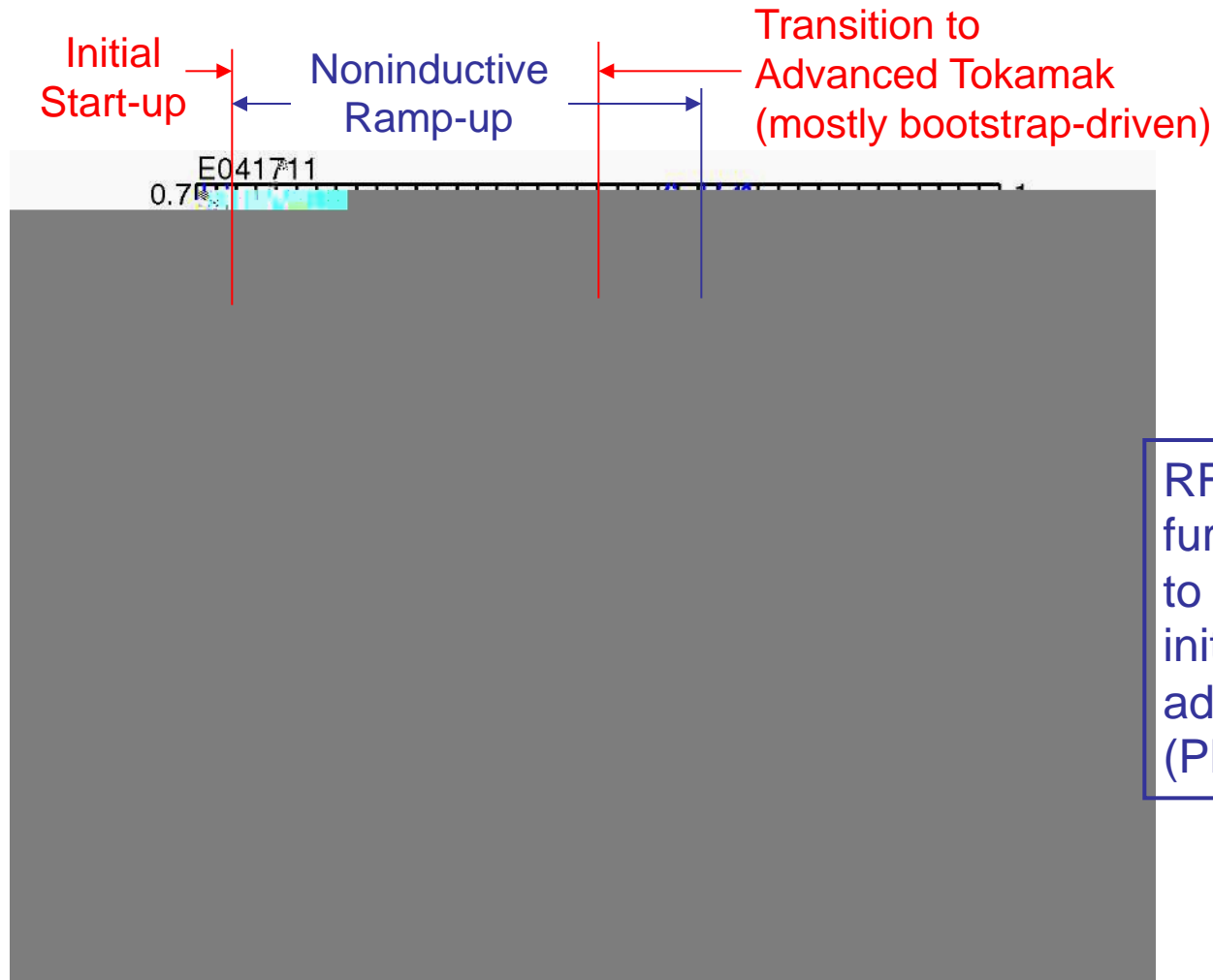
# Demonstration of Full Scenario from Start-up to Advanced

## Tokamak without OH Transformer

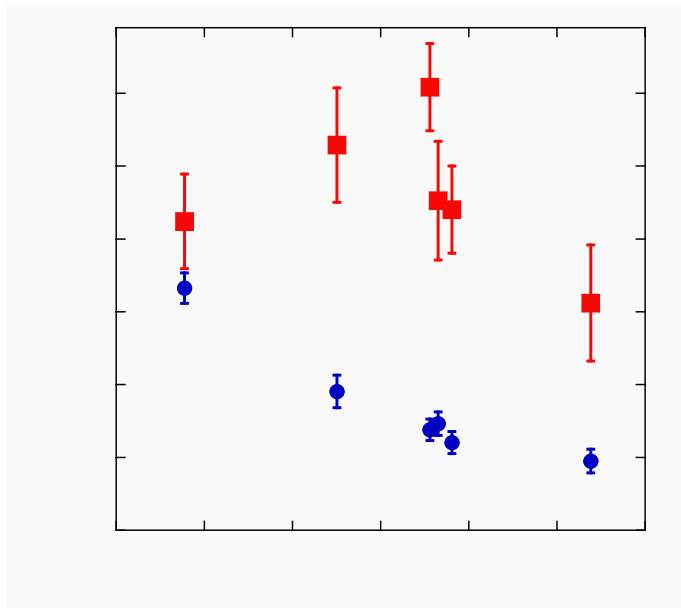
Y. Takase, et al., "IAEA 2002"

JT-60U

RFCD can be used for further current ramp-up to bridge the gap between initial start-up and NB-heated advanced tokamak phases (PLH > 1MW for JT-60U)



# TORE SUPRA: First demonstration of EC+LH synergy



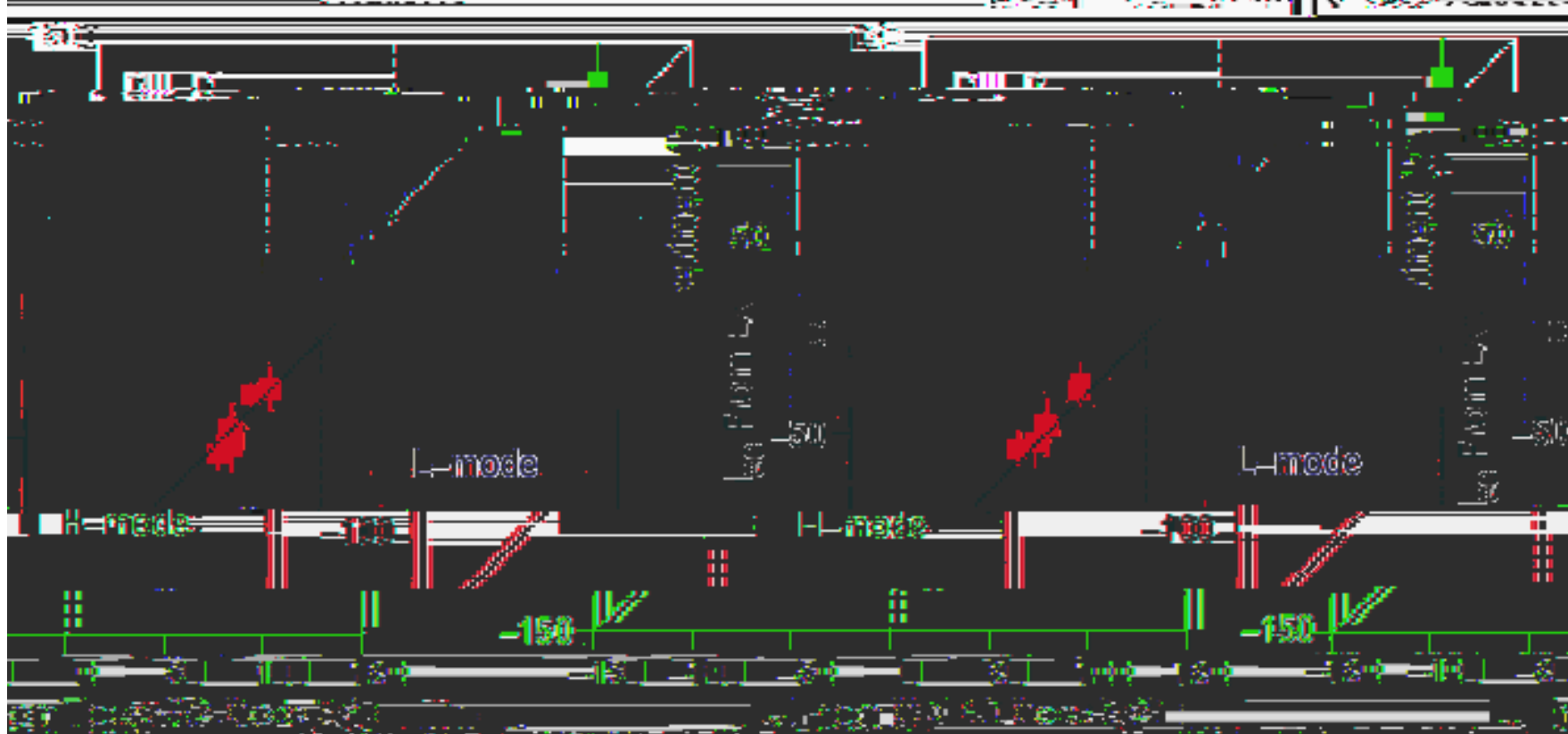


# Heating and Current Drive by Electron Cyclotron Waves

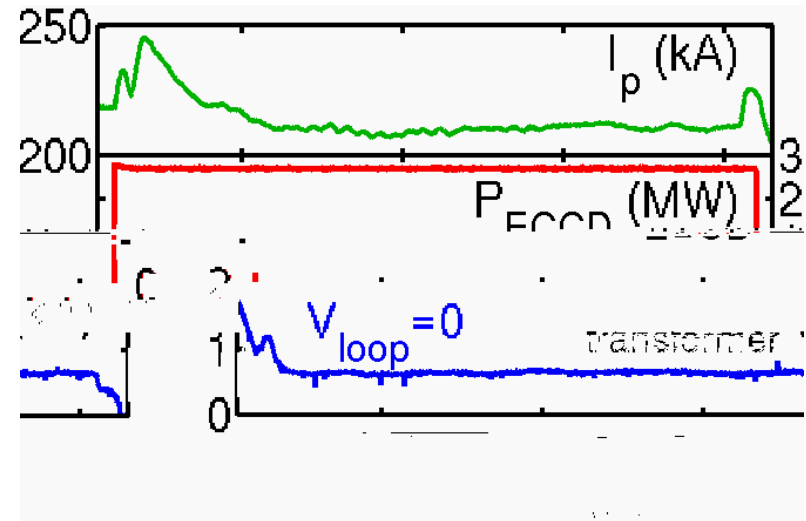
## MEASURED ECCD AGREES WITH THEORY

Fokker-Planck Code Including  
Quasilinear and E-Effects

Linear Ray-Tracing Code



# Full Steady-State Current by ECCD in TCV (record 210 kA)

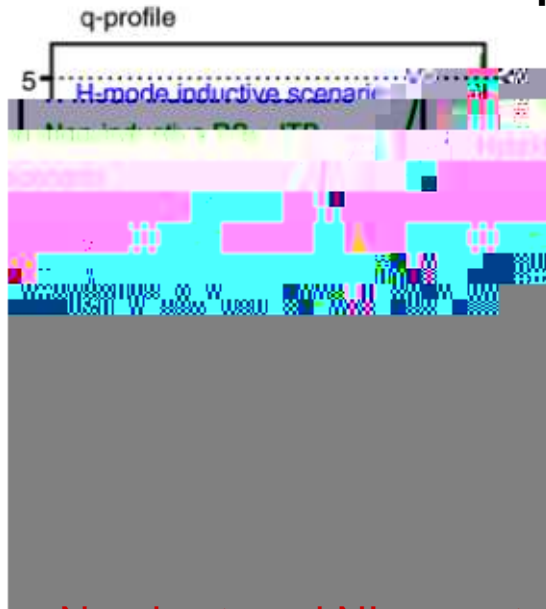


S. Coda et al. (2000)"

also e.g. *Steady-state non-inductive eITB with off-axis co-ECCD*"  
M.A. Henderson et al, Phys. Plasmas **10**, 1796 (2003)"

## ITER 'non-inductive' and 'hybrid' scenarios: rely on non-inductive (NI) current

JET Task Force S2 mission: plasmas suitable for ITER non-inductive and hybrid scenarios



*B. Green, ITER: burning plasma physics experiment, PPCF 45 (2003) 687*

### ITER 'hybrid' scenario:

~50% NI current, with ~20% self-generated bootstrap current  
candidates: plasmas with safety factor ( $q$ )  $> 1$  and  $q_{95} \sim 3-4$ ,  
with low positive or weak negative magnetic shear

### ITER 'non-inductive' scenario:

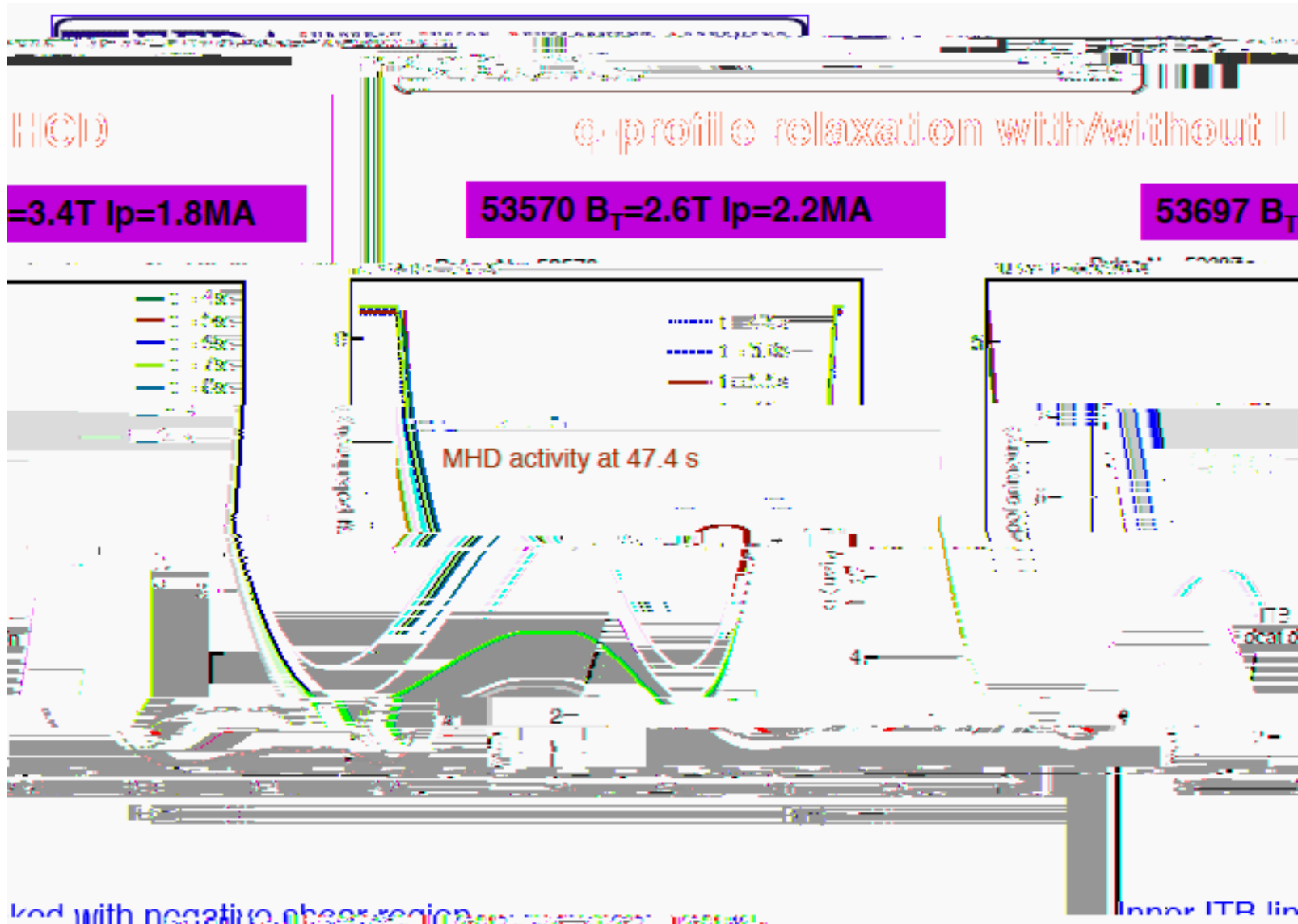
100% NI current, with  $>50\%$  BS current  
candidates: plasmas with  $q \gg 1$ ,  $q_{95} \sim 5$ , with negative magnetic shear

→ Need external NI current:

- to prepare favourable  $q$  profile
- to sustain  $q$  profile on timescale required
  - ▷ location must be compatible with current and pressure profiles, i.e. off-axis CD required

**In JET, key tool for this application is LHCD**

# JET Control of ITB with LHCD



Controlled with negative shear region

D. Mazon et al, PFCF 44 (2002) 16

**Neoclassical tearing modes reconfigure**

# New Superconducting LHCD- driven tokamaks



SST-1 India (1000 s)  
(R=1.1 m, 220 kA, 1 MW, 3.7 GHz LHCD)



EAST China (1000 s)  
(R=1.95 m, 1-1.5 MA, 4 MW, 4.6 GHz LHCD)

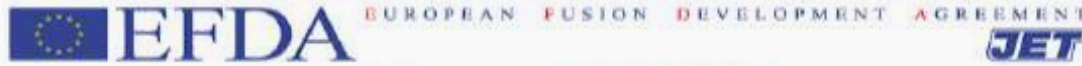


KSTAR Korea (20-300 s)  
R=1.8 m, 2 MA  
1.5 MW LHCD (2014)  
0.5 MW ECCD (2008)  
3 MW ECCD (2014)





# Minority ion Cyclotron Current Drive



Sawtooth control 



Note: MiCCD effect is complicated if  
1.! absorption straddles resonance  
2.! Ion trapping

Thus, other current drive  
effects may dominate

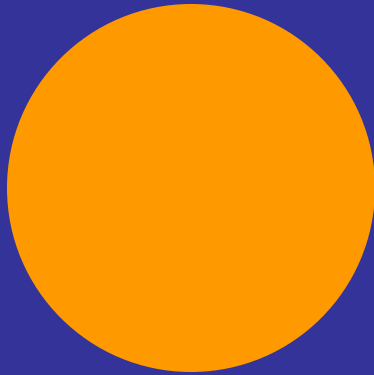
Hellsten et al., PRL, 1995  
Carlson et al., PP, 1998



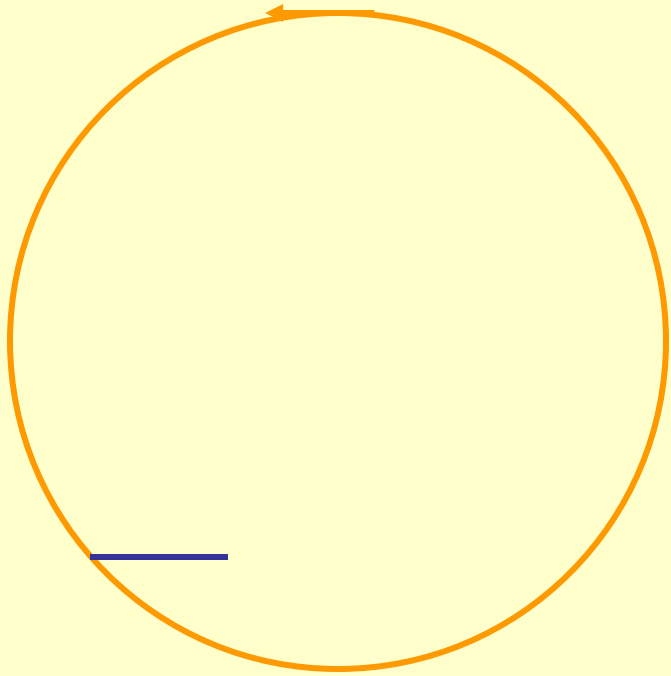


# Power Flow in a Fusion Reactor

## Advantages of "Ion-Channeling"



Get Hot Ion Mode:  $T_i > T_e$   
75% of fusion power to ions  $\Rightarrow P_f \rightarrow 2P_f$

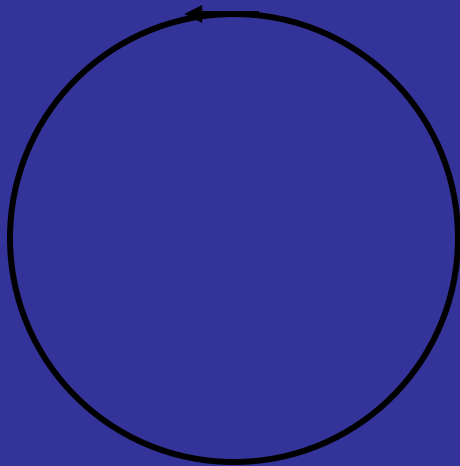
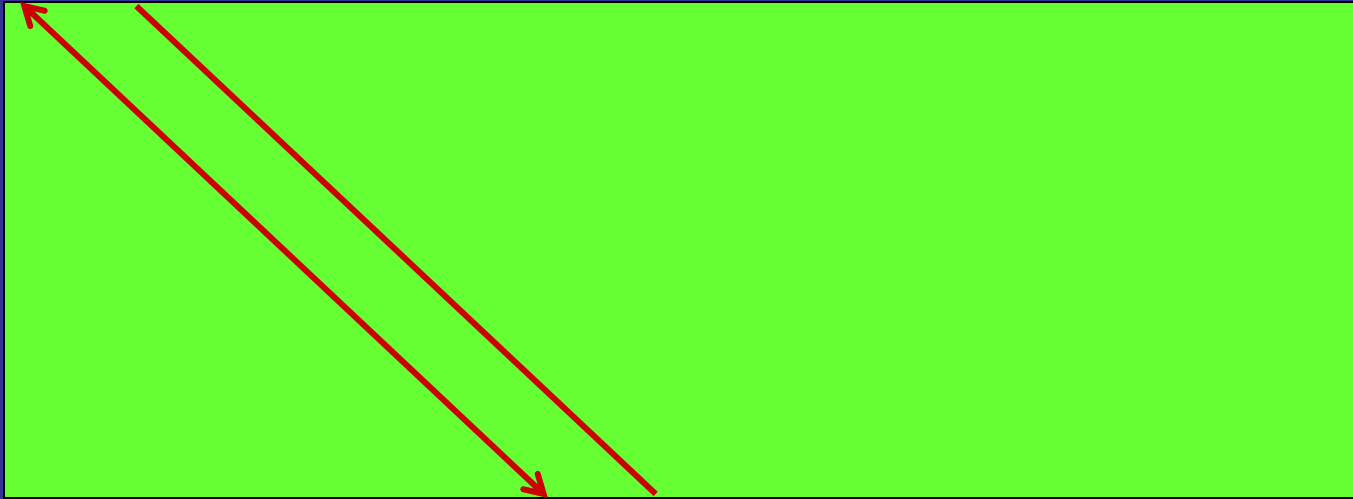


$v_y$

$v_y$

$v_y$

# Diffusion Paths



# Advantages of Alpha Channeling

- 1.! Because of the increased reactivity at a given confined pressure (and the free current drive), the hot ion mode gives about 30% cheaper COE, compared to aggressively designed reactors.
- 2.! The impurities can be removed and the plasma can be fueled easily.
- 3.! However, it may be more desirable yet, if electron heat transport is not tamed. Ion transport might eventually be tamed, but maybe not electron transport, in which case having ions hotter than electrons reduces the heat loss substantially.
- 4.! The present data base of the top tokamak confinement and heating results supports hot-ion mode operation only.

# Summary

1.!